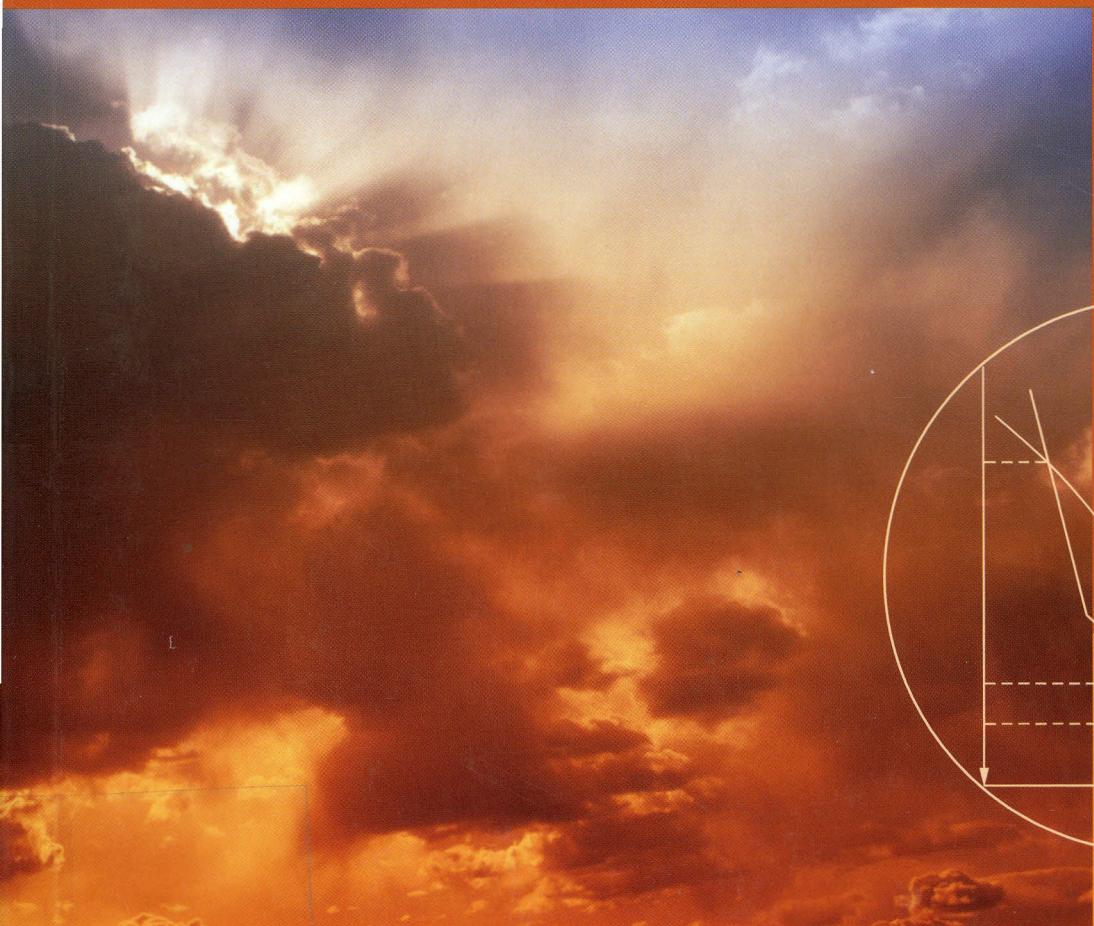


# Thermodynamics of the Atmosphere

A Course in Theoretical Meteorology



**Wilford Zdunkowski and Andreas Bott**

CAMBRIDGE

THERMODYNAMICS OF THE  
ATMOSPHERE  
A COURSE IN THEORETICAL  
METEOROLOGY

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